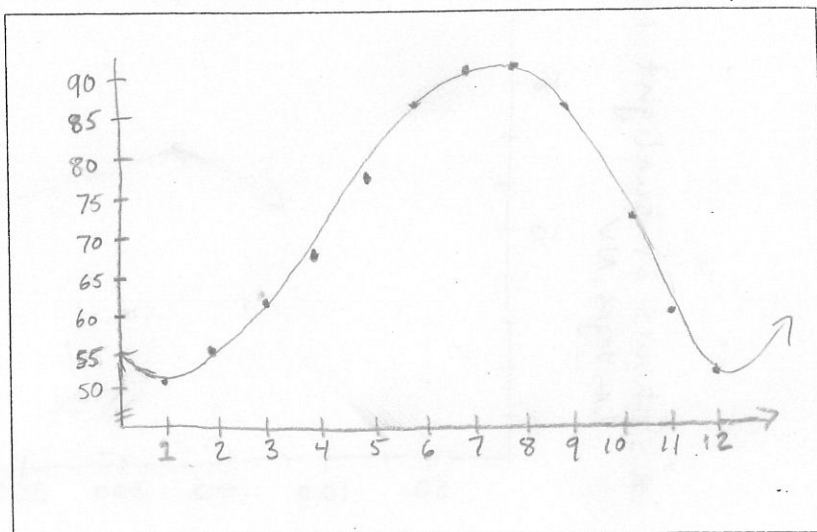


1.) The following data represent the average monthly temperatures for Phoenix, Arizona.

Month, m	Avg. Monthly Temperature, T
January, 1	51
February, 2	55
March, 3	63
April, 4	67
May, 5	77
June, 6	86
July, 7	90
August, 8	90
September, 9	84
October, 10	71
November, 11	59
December, 12	52



a.) Use a graphing utility to draw a scatter diagram of the data for one period. Make a sketch in the box above.

b.) By hand, find a sinusoidal function of the form  $y = A \sin(\omega x - \phi) + \beta$  that fits the data.

Show work below:

$d = \frac{90 + 51}{2} = 70.5$   
 $A = \frac{90 - 51}{2} = 19.5$   
 $b = \frac{2\pi}{\text{per}} = \frac{2\pi}{12} = \frac{\pi}{6}$   
 $\text{period} = 12$   
 $c = b \cdot \text{PS} = \frac{\pi}{6} \cdot 4.5 = 2.356 = C$   
 $\text{PS} \rightarrow \frac{\text{per}}{4} = \frac{12}{4} = 3 \rightarrow 7.5 - 3 = 4.5$   
 (Note:  $4.5$  is half way b/w July + Aug (both had temps of  $90^\circ$ ))

$y = 19.5 \sin\left(\frac{\pi}{6}x - 2.356\right) + 70.5$

c.) Use a graphing utility to find the sinusoidal function of best fit.  $y = 19.518(0.541x - 2.283) + 71.014$   
Round to 3 decimal places.

- STAT → Enter → Enter info from table into L<sub>1</sub> + L<sub>2</sub>
- STAT → CALC → C: Sin Reg

d.) On the diagram in the box, make a sketch of the sinusoidal function of best fit found in part c.

2.) According to the Old Farmer's Almanac, in Las Vegas, Nevada, the number of hours of sunlight on the summer solstice is 13.367 and the number of hours of sunlight on the winter solstice is 9.667.

Summer Solstice → Day 172 ; winter solstice → Day 355

a.) By hand, find a sinusoidal function of the form  $y = A \sin(\omega x - \phi) + \beta$  that fits the data.

Show work below:

$A = \frac{13.367 - 9.667}{2} = 1.85$   
 $b = \frac{2\pi}{\text{per}} = \frac{2\pi}{365}$   
 $c = b \cdot \text{PS} = \frac{2\pi}{365} \cdot 80.75 = 1.39$   
 $\text{per} = 365$   
 $\text{PS} \rightarrow \frac{365}{4} = 91.25 \rightarrow 172 - 91.25 = 80.75$   
 $d = \frac{13.367 + 9.667}{2} = 11.517$

b.) On the back of this paper, draw a graph of the function found in part a.

c.) Use the function found in part a to predict the number of hours of sunlight on April 1, the 91<sup>st</sup> day of the year.

Answer: 11.842 hrs Show work below:

$y = 1.85 \sin\left[\frac{2\pi}{365}(91) - 1.39\right] + 11.517 = 11.842 \text{ hrs}$

2b.)

